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## Iterative Reconstruction of Fluorine-18 SPECT Using Geometric Point Response Correction

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This article demonstrates resolution recovery in <sup>18</sup>F SPECT image reconstruction by using an iterative algorithm that corrects for the system geometric response. **Methods:** Patient and phantom studies were performed using a Picker PRISM 3000 three-detector SPECT system (Picker International, Inc., Cleveland, OH) to image <sup>18</sup>F with 511 keV collimators. A measured point response function of the imaging system was used in an iterative reconstruction algorithm in which the projector and backprojector modeled the system point response function by using an efficient layer-by-layer blurring technique. The blurring function was a five-element kernel in the shape of a cross. The iterative reconstruction algorithm was an ordered-subset maximum-likelihood expectation maximization algorithm. **Results:** The iterative reconstruction algorithm with geometric response correction showed an improvement in resolution over the filtered backprojection reconstruction and the iterative reconstruction without correction. **Conclusion:** The proposed iterative reconstruction algorithm with geometric response correction is efficient and effective with significant resolution recovery.

**Key Words:** fluorine-18-fluorodeoxyglucose; SPECT; geometric point response correction

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Recent efforts have used SPECT systems for imaging positron emitters such as <sup>18</sup>F. The reason has been that <sup>18</sup>F-FDG is so effective in imaging metabolism that it gives high-contrast images between viable and nonviable tissue and between malignant and benign tissue. The problem with SPECT imaging of 511 keV photons is low sensitivity due to poor geometric efficiency and poor crystal sensitivity and poor resolution due to the need for thick septum and large holes in 511 keV collimators. It is hypothesized that by modeling the spatially varying geometric response of these collimators the resolution of reconstructed SPECT images can be improved, and it may be comparable to results obtained with lower energy radiopharmaceuticals commonly used in clinical nuclear medicine.

Imaging with radioactive fluorine was first performed more than 30 yr ago. In 1962, Blau et al. (1) used a small scintillation probe to acquire images of the uptake of <sup>18</sup>F in bone. In 1965,

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Anger et al. used a positron camera (2) to perform  $^{18}\text{F}$  bone scans (3). The first peer-reviewed article on the use of  $^{18}\text{F}$ -FDG in humans was published in 1979 (4). Metabolic imaging with  $^{18}\text{F}$ -FDG has played an increasing role over the years in oncology and cardiology (5,6). Most of this imaging was performed using PET before the recent resurgence of the use of SPECT in cardiac viability studies (7–9). Even though PET outperforms SPECT in terms of sensitivity and resolution, while imaging positron emissions, SPECT is able to image multiple agents simultaneously. Another advantage of using a SPECT system is its low cost and wider availability.

This article describes a method that efficiently models the spatially varying geometric response of 511 keV collimators in the projection and backprojection operations of an iterative reconstruction algorithm. The iterative algorithm is an ordered-subset maximum-likelihood (OS-ML) expectation maximization algorithm. It is applied to SPECT data collected from patient brain and heart studies that use  $^{18}\text{F}$ -FDG and from phantom studies that use  $^{18}\text{F}$ . The algorithm performed a geometric point response correction, no correction for attenuation or scatter was implemented.

## MATERIALS AND METHODS

### SPECT Imaging System

A three-detector Picker PRISM 3000 (Picker International, Inc., Cleveland, OH) with ultrahigh-energy parallel-hole collimators was used in the  $^{18}\text{F}$  studies. The detailed collimator specification, including sensitivity/resolution measurements, can be found in an article by Lechner et al. (10). The collimators had hexagonal holes with a flat-side-to-flat-side diameter of 5.08 mm, septal thickness of 3.43 mm and holes of 77.0 mm length. The full-width at the half maximum (FWHM) at 200 mm (source-to-collimator distance) was 23 mm and at 100 mm was 17 mm as measured by a point source.

### Reconstruction Algorithm

The maximum likelihood-expectation maximization (ML-EM) algorithm is a reconstruction method commonly used in SPECT because of its unique properties of non-negativity and proper Poisson noise modeling (11). This algorithm has been used to compensate for imaging physics such as attenuation, system point spread function and scatter (12–16). The ML-EM algorithm can be expressed as:

$$x_i^{(\text{new})} = \frac{x_i^{(\text{old})} \sum_j c_{ij} P_j}{\sum_j c_{ij} \sum_k c_{kj} x_k^{(\text{old})}}, \quad \text{Eq. 1}$$

where  $x_i$  is the  $i$ th voxel in the image volume,  $P_j$  is the  $j$ th projection bin (indexing the location on the detector and the view angle of the detector) and  $c_{ij}$  is the factor that the  $i$ th voxel contributes to the  $j$ th projection bin. The summation over  $k$  is referred to as a projector, and the summation over  $j$  is called a backprojector. In this article, a rotation (14), layer-by-layer blurring projector/backprojector (17–19) was chosen.

The algorithm in Equation 1 can be implemented as an ordered-subset version (20,27). The whole set of indices  $j$  is divided into subsets, and at each image update the index  $j$  goes through only one subset. One iteration is defined as when all the subsets have been visited once. Using an ordered-subset algorithm speeds up convergence. The ordered-subset in our implementation consisted of four views, which were  $90^\circ$  apart from each other. However, it has not been proven that an ordered-subset algorithm would necessarily converge.

### Blurring Function Modeling

At each projection view, the image volume was rotated so that the face of the image volume was parallel to the detector as shown in Figure 1A. The rotation was achieved by a three-pass shear method with linear interpolation (21,22). For each layer parallel to

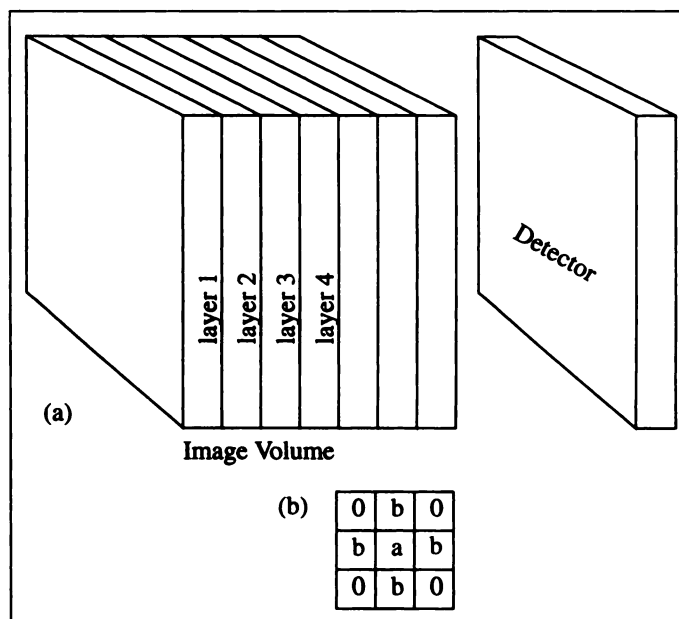


FIGURE 1. (A) The image volume is rotated to face the detector at each projection view. (B) A five-point convolution kernel is calculated for each layer.

the detector, a two-dimensional, five-point cross convolution kernel (17) was calculated according to details given in the Appendix. The incremental blurring was realized as follows: First the farthest layer from the detector (layer one in Fig. 1A) was convolved with its corresponding five-point cross convolution kernel (Fig. 1B), and the resultant two-dimensional image was added to layer two. Then, the updated layer two was convolved with its corresponding five-point cross kernel and added to layer three. This was repeated until the plane nearest the detector was reached.

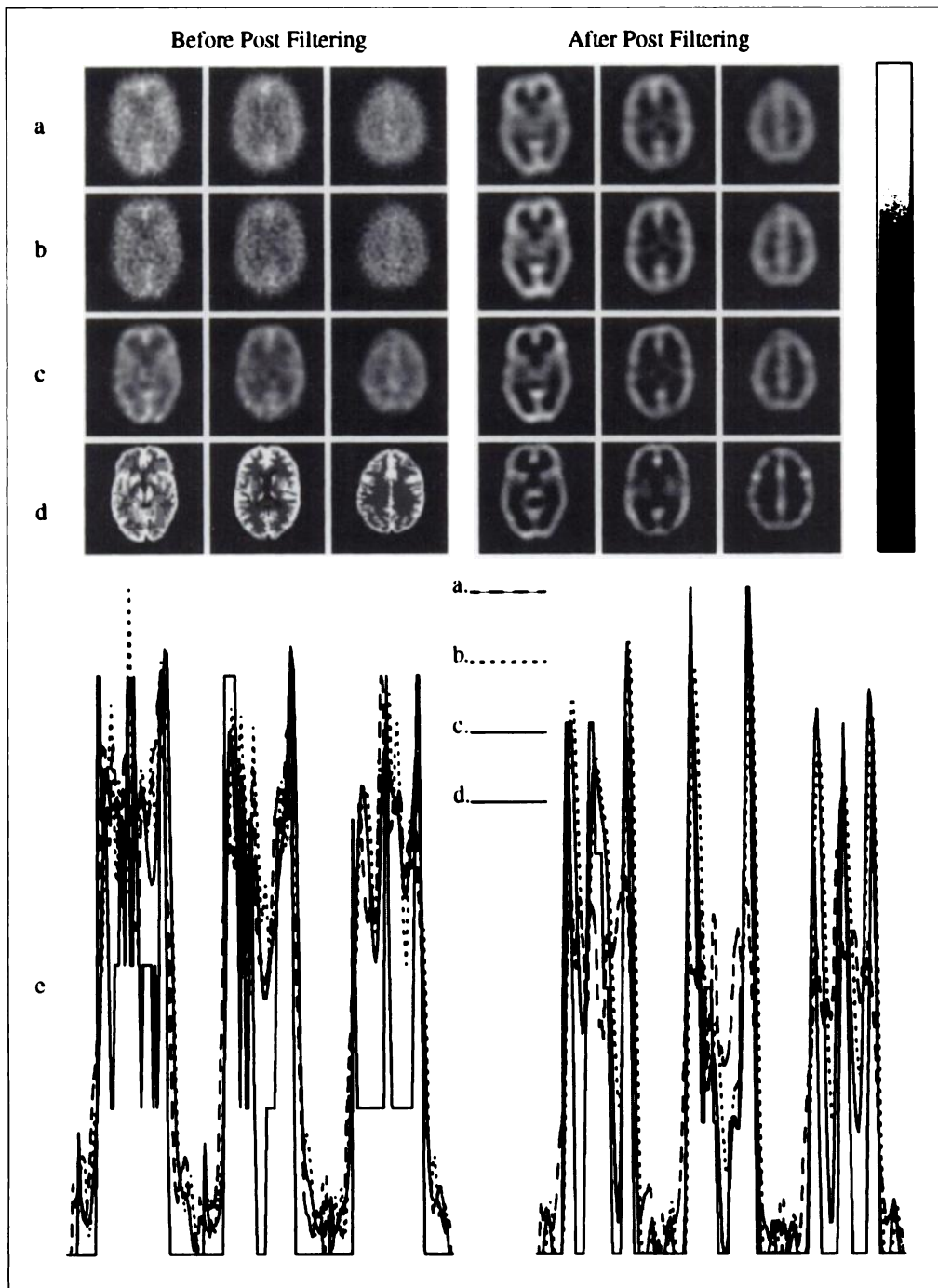
Details for calculating the five-point cross kernels are given in the Appendix. A linear relation (23) between the FWHM of the point source image and the distance from the point source to the detector was determined by fitting the multiple point response function measurements at different distances. After extracting the dimension of the  $^{18}\text{F}$  source, the resultant relation was:

$$\text{FWHM}(d) = 0.067d + 1.43, \quad \text{Eq. 2}$$

where the units of distance  $d$  and FWHM are both mm. This relation was used to calculate the five-point kernels that were used in all patient and phantom studies. Our collimator had hexagonal holes. Thus, its point-spread function was not exactly two-dimensional symmetric. Both line source and point source measurements at different distances showed that the differences between the FWHM in the horizontal and vertical directions were within 2.5%. Therefore, it was reasonable to approximate the point response as a two-dimensional symmetric function.

### Physical Hoffman Brain Phantom Studies

A shipment of  $^{18}\text{F}$  was flown from Syncor (Phoenix, Arizona) to Salt Lake City for the phantom studies. The Hoffman brain phantom (Data Spectrum Corp., Hillsborough, NC) was filled with 296 MBq (8 mCi) of  $^{18}\text{F}$  8 min before scanning. The imaging window was 15% centered at 511 keV. A continuous gantry motion was used with a total scanning time of 20 min. The distance from the center of rotation to the detector plane was 23 cm; the center of rotation to the collimator was 14 cm. The projections were acquired at 120 angles over  $360^\circ$  in  $64 \times 64$  arrays with a pixel size of 3.56 mm. Five iterations of the OS-ML algorithm was used in the reconstruction.



**FIGURE 2.** Reconstructions of  $^{18}\text{F}$  Hoffman brain phantom data using the FBP (A), the OS-ML (B) without point response correction after five iterations and the OS-ML (C) with point response correction after five iterations. Ideal bit-map representation (D). Profiles along central horizontal lines (E).

### Patient Brain Study

The data for the patient brain study were acquired at the University of Nebraska Medical Center using a Picker PRISM 3000 SPECT system. The patient (female, 53-yr-old) was injected with 370 MBq (10 mCi) of  $^{18}\text{F}$  FDG 9 min before scanning. The imaging window was 15% centered at 511 keV. The gantry motion was step-and-shoot. A circular scanning orbit was used, and the detector radius was 25.61 cm. The projections from the three detectors were acquired at 120 angles over 360°. There were 40 stops with 60 sec at each stop giving a total scanning time of 44 min. The projection data were stored in 120  $64 \times 64$  arrays with a pixel size of 7.12 mm in both horizontal and vertical directions. All the iterative reconstructions used five iterations.

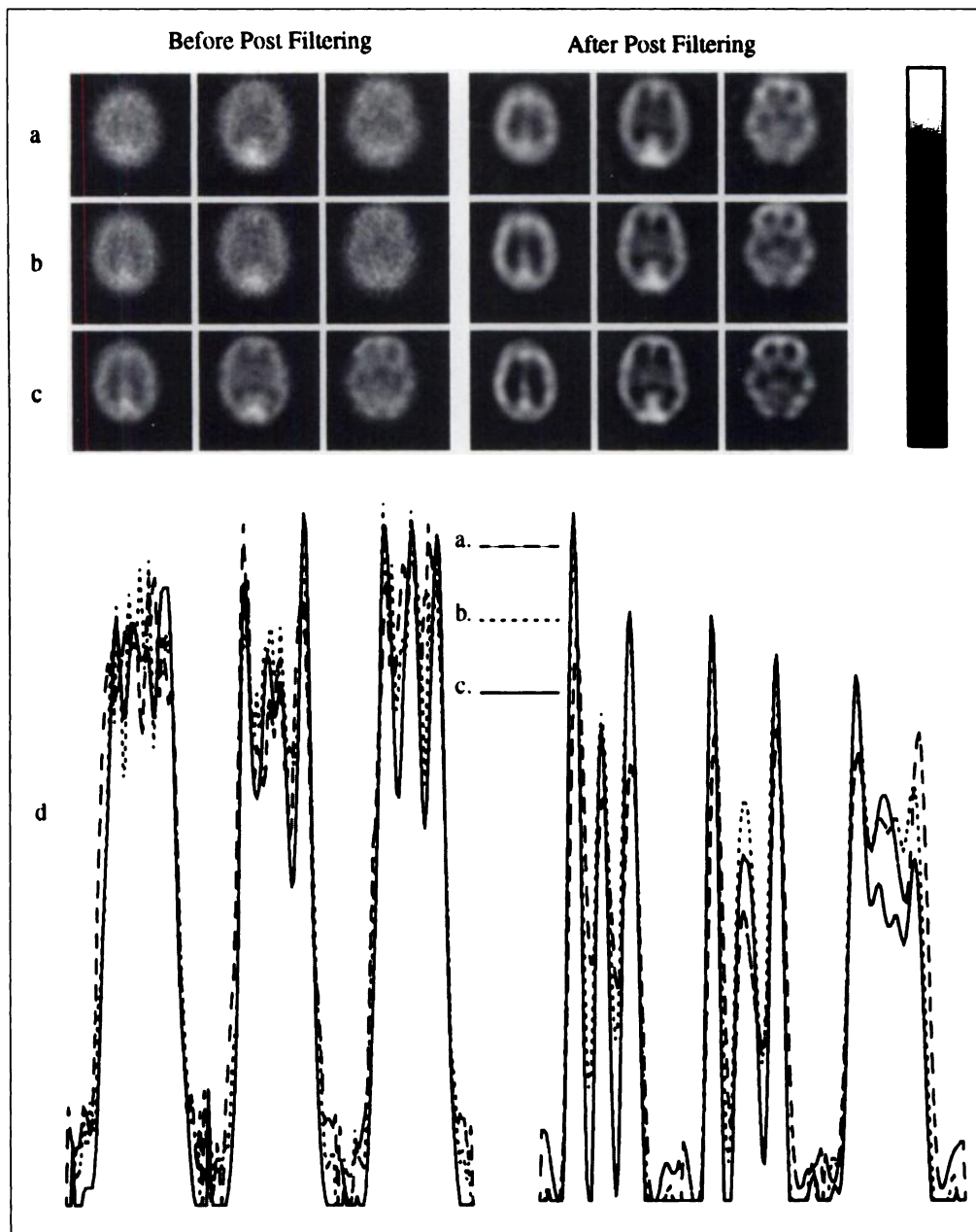
### Patient Cardiac Study

The data for the patient cardiac study were acquired at the AZR Dijkzigt Hospital in Rotterdam, The Netherlands, with a Picker

PRISM 3000 SPECT system. The patient (male, 73-yr-old) was injected with 222 MBq (6 mCi) of  $^{18}\text{F}$  FDG 3 min before scanning. The imaging window was 15% centered at 511 keV. A noncircular scanning orbit was used with a detector radius of approximately 30 cm. The gantry motion was continuous with a total scanning time of 33 min. The projections were acquired at 120 angles over 360° into  $64 \times 64$  arrays with a pixel size of 4.45 mm in both horizontal and vertical directions. Five iterations were used in all the iterative reconstructions.

### RESULTS

Figures 2–4 show the transverse views of the reconstructions from the Hoffman brain phantom data, the patient brain data and the patient cardiac data, respectively. All three sets of images show the filtered backprojection reconstruction in A, the iterative reconstruction without system point response compen-



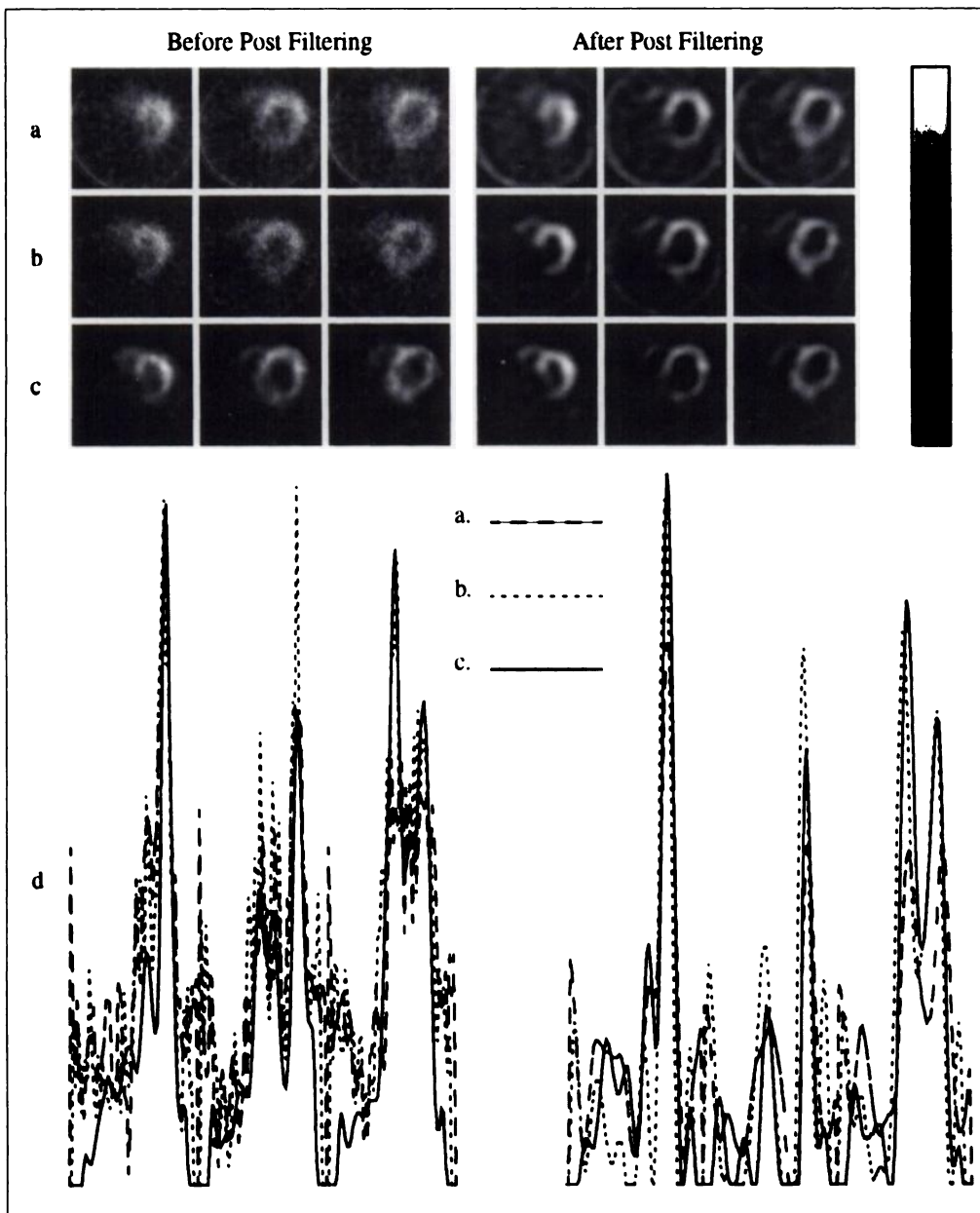
**FIGURE 3.** Reconstructions of  $^{18}\text{F}$ -FDG patient brain data using the FBP (A), the OS-ML (B) without point response correction after E5 iterations and the OS-ML (C) with point response correction after five iterations. Profiles along the central horizontal lines (D).

sation in B and the iterative reconstruction with system point response compensation in C. The collimators had thick septa of 3.43 mm, and a black septal pattern could be clearly visualized in the projection data. To remove the pattern, all of the projections were first low-pass filtered before reconstruction as suggested in Lechner et al.'s article (10). The low-pass prefilter was an averaging filter. A  $3 \times 3$  kernel was used, and its values were  $1/9$  for each cell in the kernel. Note that the point response measurements were also first low-pass filtered before they were used to estimate the system FWHM functions. A three-dimensional Metz postfilter (24) was applied to all the reconstructions on the left. The filtered images are shown on the right. To show the ideal images of the Hoffman brain phantom, a bit-map is shown in Figure 2D. The computation time for each slice ( $64 \times 64$ ) was 2 sec per iteration using one processor on a Sun Ultra Enterprise 3000 workstation (Milpitas, CA) (four processors at 167 MHz each).

## DISCUSSION

FDG patient brain and heart SPECT studies and  $^{18}\text{F}$  phantom SPECT studies were performed using Picker PRISM 3000 SPECT systems at various facilities with parallel-hole collimators specially designed for 511 keV. The iterative reconstructions with the OS-ML algorithm with system point response correction were compared with filtered backprojection reconstructions and iterative reconstruction without system point response correction. The projector and backprojector in the iterative reconstruction algorithm used a layer-by-layer incremental blurring scheme to model the distance-dependent collimator geometric point response function. On a Sun Ultra Enterprise 3000 workstation, the iterative algorithm required 2 sec per iteration for each ( $64 \times 64$ ) slice. The reconstructions from the iterative algorithm with collimator geometric point response correction showed improved resolution over the filtered backprojection results and iterative algorithm results without collimator geometric point response correction.





**FIGURE 4.** Reconstructions of  $^{18}\text{F}$ -FDG patient cardiac data using the FBP (A), the OS-ML (B) without point response correction after five iterations and the OS-ML (C) with point response correction after five iterations. Profiles along the central horizontal lines (D).

A small  $3 \times 3$  two-dimensional low-pass filter was applied to all projection data to remove the collimator hole pattern, as suggested in Lechner et al.'s article (10), and to remove some high-frequency noise. Because this prefiltering is linear and shift-invariant, it can be incorporated in the overall system point response function. Therefore, any resolution loss because of prefiltering can also be modeled during the iterative reconstruction procedure.

It is observed that the iterative reconstruction with geometric point response correction allows smoothing without loss of resolution. In this article, both the filtered backprojection algorithm and the iterative reconstruction algorithm used the same sets of slightly low-pass filtered projection data. However, the filtered backprojection and iterative reconstructions without corrections were much noisier than those obtained from the iterative reconstructions with depth-dependent point response correction. This is partially because the projector and backprojector that modeled the geometric point response inherently contained a blurring function that reduced the high-frequency noise. Of course, the high-frequency noise can also be suppressed by a linear three-dimensional postfilter (24). For exam-

ple, a three-dimensional post-Metz filter can improve the image quality significantly. A Metz filter suppresses the high-frequency noise and enhances the midfrequency components. However, some clinically important high-frequency details can also be suppressed by using a Metz filter. The reconstructions with depth-dependent point response correction produce improved resolution over that of the reconstructions without the correction.

The iterative algorithms used to correct for system point response have improved tremendously in computation time over the last few years. A ray-tracing projector/backprojector was originally implemented (12) that required 100 iterations of an EM-ML algorithm to obtain a result comparable to that obtained with five iterations of the OS-ML algorithm. Total reconstruction time for a  $64 \times 64 \times 64$  image array was 400 hr on an IBM 3090 computer (12). The algorithm was later made 50 times faster (total reconstruction time was 8 hr) by rotating the image as done currently and calculating the blurring for each layer by applying a full convolution kernel in the frequency domain, which modeled the effect of the point response function at that layer (13). The new proposed algorithm can

reconstruct a  $64 \times 64 \times 64$  image array with system point response correction in about 10 min on a Sun Ultra Enterprise 3000 workstation by using incremental small convolution kernels and only five iterations of the OS-ML algorithm, due to its fast convergent property.

It is observed in studying the feasibility of using SPECT to image  $^{18}\text{F}$ -FDG that it is necessary to correct for the spatially varying geometric point response of the 511 keV collimators in order to obtain images comparable to those obtained with low energy radiopharmaceuticals commonly used in the clinic. The proposed reconstruction technique improves the contrast, which is expected to increase lesion detectability in clinical diagnosis. In addition, resolution recovery will be especially important for quantitative studies, such as those that use dynamic SPECT, where bias of kinetic parameters is significantly affected by resolution.

In iterative algorithms, each iteration can be treated as applying a spatially variant filter to the image. The resolution recovery varies for different frequency components and for different parts of the image. Their nonlinear nature makes the frequency response and noise propagation of iterative algorithms more difficult to study than in analytical algorithms. Other researchers have made significant progress in using analytical algorithms to correct for depth-dependent blurring and uniform attenuation (25,26); however, these algorithms cannot handle nonuniform attenuation and scatter.

## CONCLUSION

The proposed iterative reconstruction algorithm with geometric response correction is efficient and effective with significant resolution recovery. Post-filtering is not encouraged because it suppresses clinically important high-frequency details while suppressing noise.

## APPENDIX

The five-point cross convolution kernels used in the incremental layer-by-layer blurring are derived. The kernels are approximated from Gaussian point spread functions, which are used to model the spatially varying point response of the 511 keV parallel collimators/camera system. For parallel collimators, the s.d. of these Gaussians is a linear function of the distance from the point source to the detector (23).

If two measurements of the FWHM,  $w_1$  and  $w_2$ , are made at two distances,  $d_1$  and  $d_2$ , respectively, the s.d. of the point spread function at distance  $d$  is (23):

$$\hat{\sigma}_d = \alpha d + \hat{\sigma}_0, \quad \text{Eq. A1}$$

where

$$\alpha = \frac{(w_1 - w_2)/\sqrt{8 \ln 2}}{d_1 - d_2}, \quad \text{Eq. A2}$$

and

$$\hat{\sigma}_0 = w_1/\sqrt{8 \ln 2} - d_1\alpha. \quad \text{Eq. A3}$$

Here  $1/\sqrt{8 \ln 2}$  is the conversion factor to convert a FWHM to a Gaussian s.d. For the 511 keV collimators used in this article, the linear function in Equation A1 was calculated by using  $d_1 = 23$  cm,  $w_1 = 1.84$  cm,  $d_2 = 0$  cm and  $w_2 = 0.38$  cm.

Incremental layer-by-layer blurring is implemented by a series of convolutions starting with the layer farthest from the detector:

$$\begin{aligned} \text{projection} = & \{[(\text{layer}_1 * h_1 + \text{layer}_2) * h_2 + \text{layer}_3] * \\ & h_3 + \text{layer}_4\} * h_5 + \dots, \end{aligned} \quad \text{Eq. A4}$$

where  $*$  denotes the two-dimensional convolution. Each  $h_k$  is a two-dimensional convolution kernel with a variance  $\sigma_k^2$ . If  $s$  is the

layer thickness, and if layer  $k$  is at a distance  $d$ , then the variance  $\sigma_k^2$  is:

$$\sigma_k^2 = \hat{\sigma}_d^2 - \hat{\sigma}_{(d-s)}^2, \quad \text{Eq. A5}$$

where  $\hat{\sigma}_d^2$  is the variance of the Gaussian point spread function at the distance  $d$ , and  $\hat{\sigma}_{(d-s)}^2$  is the variance of the Gaussian point spread function at the distance  $d-s$  away from the collimator. This follows from the fact that the convolution of two Gaussians is a Gaussian with a variance equal to the sum of the variances of each Gaussian. Using Equation A1, the expression for  $\sigma_k^2$  in Equation A5 becomes:

$$\sigma_k^2 = d(2s\alpha^2) + (2s\alpha\hat{\sigma}_0 - \alpha^2s^2). \quad \text{Eq. A6}$$

This gives an expression for the variance of the convolution kernel  $h_k$ , which is the incremental blurring applied in summing layer  $k$  to layer  $k-1$ .

In the algorithm implementation, the convolution kernel  $h_k$  is approximated by a five-point cross-kernel of the following form:

0	b	0
b	a	b
0	b	0

Eq. A7

with the normalization constraint that the sum of the kernel entries is unity, yielding

$$b = \frac{1-a}{4} \quad \text{for } 0 < a \leq 1. \quad \text{Eq. A8}$$

Assume that the system point response function is Gaussian. Let

$$f_1(x, y) = \frac{1}{\sqrt{2\pi\sigma_1^2}} \exp\left(-\frac{x^2 + y^2}{2\sigma_1^2}\right) \quad \text{Eq. A9}$$

be the point spread function at distance  $d$  and

$$f_2(x, y) = \frac{1}{\sqrt{2\pi\sigma_2^2}} \exp\left(-\frac{x^2 + y^2}{2\sigma_2^2}\right) \quad \text{Eq. A10}$$

be the point spread function at distance  $d + s$ . If  $f_2$  can be approximated by convolving  $f_1$  with the kernel defined in Equation A7, then

$$\begin{aligned} f_2(x, y) \approx & af_1(x, y) + b[f_1(x+1, y) + f_1(x-1, y) + f_1(x, y+1) \\ & + f_1(x, y-1)]. \end{aligned} \quad \text{Eq. A11}$$

Using Equations A8-A11 becomes

$$t_3 \approx at_1 + \frac{1-a}{4}t_2, \quad \text{Eq. A12}$$

where

$$t_1(x, y) = \exp\left(-\frac{x^2 + y^2}{2\sigma_1^2}\right), \quad \text{Eq. A13}$$

$$\begin{aligned} t_2(x, y) = & \exp\left(-\frac{(x+1)^2 + y^2}{2\sigma_1^2}\right) + \exp\left(-\frac{(x-1)^2 + y^2}{2\sigma_1^2}\right) \\ & + \exp\left(-\frac{x^2 + (y+1)^2}{2\sigma_1^2}\right) + \exp\left(-\frac{x^2 + (y-1)^2}{2\sigma_1^2}\right) \end{aligned} \quad \text{Eq. A14}$$

$$t_3(x, y) = \frac{\sigma_1}{\sigma_2} \exp\left(-\frac{x^2 + y^2}{2\sigma_1^2}\right). \quad \text{Eq. A15}$$

To find the parameter  $a$ , it is necessary to minimize the following cost function  $F$ :

$$F(a) = \sum_x \sum_y \left[ a t_1(x, y) + \frac{1-a}{4} t_2(x, y) - t_3(x, y) \right]^2 \quad \text{Eq. A16}$$

Setting the first derivative of F(a) to zero, parameter a is obtained as:

$$a = \frac{\sum_x \sum_y (t_3 - t_2/4)(t_1 - t_2/4)}{\sum_x \sum_y (t_1 - t_2/4)^2} \quad \text{Eq. A17}$$

Once parameter a is obtained, parameter b is calculated via Equation A8.

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## Pinhole SPECT Imaging in Normal and Morbid Ankles

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Pinhole SPECT can generate sectional nuclear images of a normal and morbid ankle and hindfoot with remarkably enhanced resolution by portraying the topography and pathological alterations in great detail. **Methods:** Pinhole SPECT was performed using a commercially available single-head, rotating gamma camera system by replacing the parallel-hole collimator used for planar SPECT with a pinhole collimator. The images were reconstructed in the same way as in planar SPECT by using the filtered back-projection algorithm and a Butterworth filter. First, we compared the scan resolution between the planar and pinhole SPECT images of a thyroid phantom and a normal ankle and hindfoot by working out pinhole SPECT anatomy with CT validation. Second, the clinical usefulness was assessed in one case each of fracture, reflex sympathetic dystrophy

syndrome and rheumatoid arthritis of the ankle with radiographic correlation. The resolution of the pinhole SPECT and planar pinhole images was compared for these diseases. **Results:** The resolution of the pinhole SPECT of a thyroid phantom and of a normal ankle and hindfoot was significantly enhanced compared to the planar SPECT although image distortion was seen in the periphery of the field-of-view. The pinhole SPECT resolution was such that most of the anatomical landmarks were sharply delineated in the ankle and hindfoot and some useful diagnostic signs in the diseased ankle were visible. **Conclusion:** Pinhole SPECT can be performed using a single-head gamma camera system and filtered back-projection algorithm. It generates sectional scan images of both normal and morbid ankle and hindfoot with enhanced resolution portraying many anatomical landmarks and pathological signs in useful detail.

**Key Words:** SPECT; pinhole; bone; ankle

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